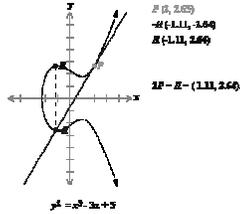


CNS Lecture 9

Security through mathematics

- more public key crypto
- ECC
- Applied crypto
- ssh
- pgp
- PKI



Assignment 8 due 10/28/06



You are here ...

Attacks & Defenses	Cryptography	Applied crypto
<ul style="list-style-type: none"> Risk assessment ✓ Viruses ✓ Unix security ✓ authentication ✓ Network security Firewalls, vpn, IPsec, IDS Forensics 	<ul style="list-style-type: none"> Random numbers ✓ Hash functions ✓ MD5, SHA, RIPEMD Classical + stego ✓ Number theory ✓ Symmetric key ✓ DES, Rijndael, RC5 Public key RSA, DSA, D-H, ECC 	<ul style="list-style-type: none"> SSH PGP S/Mime SSL Kerberos IPsec Crypto APIs Coding securely

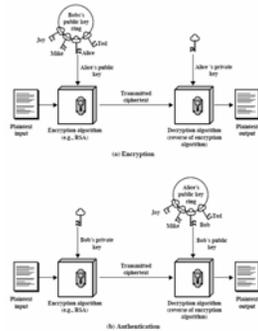
CNS Lecture 9 - 2



Public key crypto

- Diffie-Hellman key establishment**
 - Discrete logs
 - $X = g^x \text{ mod } p$
- RSA**
 - Factoring integers, $n = pq$
 - $c = m^e \text{ mod } n$
- DSA**
 - Discrete logs, sign only
- ECC**

BIG integers (1000-bit)



CNS Lecture 9 - 3



OpenSSL

- `genrsa, gendh, gendsa` -- generate keys
`genrsa -des3 -out ca.key 1024`
- `rsautl` -- encrypt/decrypt sign/verify
- Plus the hash (md5, sha) and encrypt (AES, DES) commands
- API for doing rand, big numbers, find prime, D-H, encrypt/decrypt, sign/verify

CNS Lecture 9 - 4



ECC – elliptic curve cryptography

- Based on elliptic curve arithmetic (old field of mathematics)
- Form of public key encryption
 - More security per bit than any other public key crypto
 - Efficient hardware implementations
 - Suitable for cryptocards, cell phones, PDAs
 - Free software (few? licensing restrictions)
 - Strength not based on factoring (just in case ☹)
 - Strength/operation similar to Diffie-Hellman
 - Mathematics more complex than RSA/D-H, so smaller keys and faster (10x) in hardware

CNS Lecture 9 - 5



Stacking balls

- Great moments in elliptic curves
- How many balls do you need to stack in the arrangement 1 on top of 4 on top of 9 on top of 16 ...
 $1^2 + 2^2 + 3^2 + 4^2 \dots + x^2$ so that they form a perfect square when collapsed? The sum is $x(x+1)(2x+1)/6$
- So you want $y^2 = (2x^3 + 3x^2 + x)/6$ an elliptic curve!



Lots of (x,y) solutions, including negative and fractional tennis balls, but only two solutions in whole tennis balls! ☺
(1,1) or (24,70)
4900 balls in a pyramid 24 balls high, or 70 by 70 square

CNS Lecture 9 - 6



Elliptic curves

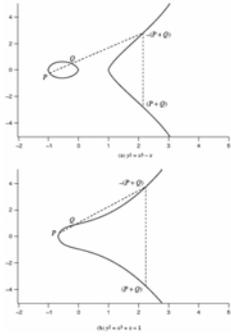
- Elliptic curves are NOT ellipses
- Described by cubic equations of the form $y^2 = x^3 + ax + b$ $E(a,b)$
 $P = (x,y)$ is a point on the curve if (x,y) is in $E(a,b)$
 $-P = (x, -y)$
forms a group over addition if $(4a^3 + 27b^2) \neq 0$ there is an additive identity O
- Addition over $E(a,b)$ (geometric)
 $P + Q$ where P and Q are points in $E(a,b)$
Draw line thru P and Q , where line intersects curve (R), the result is the mirror image (reflection) of R

Algebraically

$$x_R = \lambda^2 - x_P - x_Q$$

$$y_R = -y_P + \lambda(x_P - x_Q)$$

where $\lambda = (y_Q - y_P)/(x_Q - x_P)$



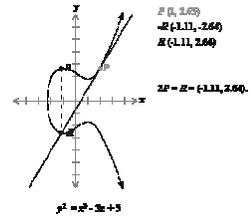
CNS Lecture 9 - 7

Elliptic curve addition

- To double a point, $P+P = 2P = R$, (geometric) draw a tangent to P , its reflection is R
- Multiplication is defined as repeated additions $nP = P+P+\dots+P$
- Algebraically

$$x_R = \left(\frac{3x_P^2 + a}{2y_P} \right)^2 - 2x_P$$

$$y_R = \left(\frac{3x_P^2 + a}{2y_P} \right) (x_P - x_R) - y_P$$



Cerlicom's [ECC tutorial](#)

CNS Lecture 9 - 8

Elliptic curves over Z_p

Equations of form (prime curves)

$$y^2 \bmod p = (x^3 + ax + b) \bmod p \quad E_p(a,b)$$

forms a group over addition if $(4a^3 + 27b^2) \bmod p \neq 0$ (p is a BIG prime)
Variables and coefficients are in the set of integers $[0 \dots p-1]$

Rules for addition:

$$x_R = (\lambda^2 - x_P - x_Q) \bmod p$$

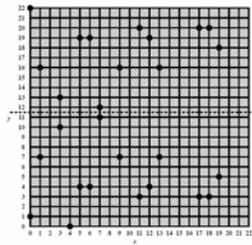
$$y_R = (\lambda(x_P - x_Q) - y_P) \bmod p$$

where $\lambda = (y_Q - y_P)/(x_Q - x_P) \bmod p$ if $P \neq Q$
or $\lambda = (3x_P^2 + a)/(2y_P) \bmod p$ if $P = Q$

Example: $E_{23}(1,1)$

$$y^2 = x^3 + x + 1 \bmod 23$$

(0, 3)	(6, 4)	(12, 19)
(8, 22)	(6, 19)	(13, 7)
(1, 7)	(7, 13)	(13, 16)
(1, 16)	(7, 12)	(17, 3)
(3, 10)	(8, 7)	(17, 20)
(3, 13)	(9, 10)	(18, 3)
(4, 6)	(11, 3)	(18, 20)
(5, 4)	(11, 20)	(19, 5)
(5, 19)	(12, 4)	(19, 18)



CNS Lecture 9 - 9

For real crypto, BIG integers (160 bits)

ECC encryption

- $E_p(a,b)$ and point G are published
- each user selects random private key n , public key is $K_p = n_p G$
- encode message as a point M on the curve (tricky but doable, FKCS #13)
- Alice encrypts M to Bob using Bob's public key K_b
generate random r , send the following message to Bob
 $C_m = \{X, Y\}$ where $X = rG$ and $Y = M + rK_b$
- Bob decrypts by calculating
 $Y - n_b X = M + rK_b - n_b rG = M + r(n_b G - n_b rG) = M$
- Easy to calculate $X = rG$
attacker has to find r given X and G -- real hard for large 160-bit primes!
-- Sort of discrete logarithm problem for elliptic curves
-- Repeated additions (rather than multiplications as in D-H)
-- Best method to find k given X , use Pollard Rho method, exponential time algorithm with complexity $O(\sqrt{n})$

CNS Lecture 9 - 10

ECC discrete logs



In the elliptic curve group defined by

$$y^2 = x^3 + 9x + 17 \text{ over } F_{25}$$

What is the discrete logarithm k of $Q = (4,5)$ to the base $P = (16,5)$?

One (brute force) way to find k is to compute multiples of P until Q is found. The first few multiples of P are:

$$P = (16, 5) \quad 2P = (20, 20) \quad 3P = (14, 14) \quad 4P = (19, 20) \quad 5P = (13, 10)$$

$$6P = (7, 3) \quad 7P = (8, 7) \quad 8P = (12, 17) \quad 9P = (4, 5)$$

Since $9P = (4, 5) = Q$, the discrete logarithm of Q to the base P is $k = 9$.

In a real application, k and the modules would be large enough (e.g. 160 bits) such that it would be infeasible to determine k in this manner.

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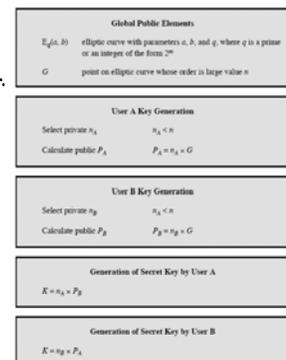
ECC key establishment

D-H equivalent, though 5 to 10 times faster.
 n "additions" rather than n multiplications

The "generator", base point, G , has a high order, $nG = O$ (n is large)

Algorithms/encodings:

- FKCS 13
- ANSI X9.62 X9.63
- ECDH in OpenSSL (eal)



CNS Lecture 9 - 12

ECC digital signatures

- TLS and OpenSSL ECDSA
- Algorithm like DSA, generate a verifier of the hash of message
- Sign:
 - Given equation info $E_p(a,b)$ and base point G order n
 - given message hash h
 - Given Alice's private/public key k_A and Q_A (where $Q_A = k_A G$)
 - Generate big random integer z and point on curve $Z = zG = (x,z)$
 - set $r = x \bmod n$ and $s = z^{-1}(h + rk_A) \bmod n$
 - Send message and verifier pair r and s
- Verify
 - Regenerate hash h' , calculate $u_1 = h's^{-1}$ $u_2 = rs^{-1} \bmod n$
 - Calculate point on curve $Z' = u_1G + u_2Q_A$
 - $Z' = Z$ if $h = h'$ → verified hash the same

$$u_1G + u_2Q_A = h's^{-1}G + rs^{-1}k_A G = h'z(h+rK_A)^{-1}G + rz(h+rK_A)^{-1}k_A G$$

$$= zG(h+rK_A)^{-1}(h' + rk_A)$$

$$= zG \rightarrow \text{a point } (x', y')$$

signature valid if $x' \bmod n = r$

CNS Lecture 9 - 13

Elliptic curves over $GF(2^m)$

polynomial arithmetic (again!), cubic equation where variables and coefficients are all in $GF(2^m)$ ($m=160$ for today's crypto)

$$y^2 + xy = x^3 + ax^2 + b \quad (\text{group if } b \text{ is non-zero})$$

Rules for addition: (uses polynomial arithmetic)

$$P \neq Q \quad \begin{aligned} x_R &= \lambda^2 + \lambda + x_P + x_Q + a \\ y_R &= \lambda(x_P + x_Q) + x_Q + y_P \end{aligned} \quad \begin{aligned} P &= Q \\ x_R &= \lambda^2 + \lambda + a \\ y_R &= x_P^2 + (\lambda+1)x_P \end{aligned}$$

where $\lambda = (y_Q + y_P) / (x_Q + x_P)$ where $\lambda = x_P + y_P / x_P$

- Efficient in hardware (add is XOR, multiply is shifts and XORs)

Certicom's [ECC tutorial](#)

Orthonormal basis is even faster in hardware for squaring (just a rotate).

CNS Lecture 9 - 14

Poly arithmetic over $GF(2^4)$

$$\begin{aligned} g^0 &= (0001) & g^1 &= (0010) & g^2 &= (0100) & g^3 &= (1000) \\ g^4 &= (0011) & g^5 &= (0110) & g^6 &= (1100) & g^7 &= (1011) \\ g^8 &= (0101) & g^9 &= (1010) & g^{10} &= (0111) & g^{11} &= (1110) \\ g^{12} &= (1111) & g^{13} &= (1101) & g^{14} &= (1001) & g^{15} &= (0001) \end{aligned}$$

- Mod irreducible polynomial ($x^4 + x + 1$)
- Elements of set are $\{0000, 0001, 0010, 0011, \dots, 1111\}$
- Addition and subtraction just XOR
- Multiplication is done $\bmod x^4 + x + 1$
- generator g (e.g. 0010) is an element whose powers g^i generate the entire set
- Multiplicative inverse of g^i is $g^{-i \bmod 15}$

$g^7 = 1011$ $g^{-7 \bmod 15} = g^8 = 0101$, to check
does $1011 \times 0101 = 0001$?
 $(x^3 + x + 1)(x^2 + 1) \bmod (x^4 + x + 1)$
 $x^5 + x^2 + x + 1$ (divide by $x^4 + x + 1$), get
remainder of 1, so g^7 is multiplicative inverse of g^8

CNS Lecture 9 - 15

ECC over $GF(2^4)$ -- example

- Irreducible polynomial $x^4 + x + 1$
- generator $g = (0010)$
- Elliptic curve
 $y^2 + xy = x^3 + g^4x^2 + 1$

$$\begin{aligned} g^0 &= (0001) & g^1 &= (0010) & g^2 &= (0100) & g^3 &= (1000) \\ g^4 &= (0011) & g^5 &= (0110) & g^6 &= (1100) & g^7 &= (1011) \\ g^8 &= (0101) & g^9 &= (1010) & g^{10} &= (0111) & g^{11} &= (1110) \\ g^{12} &= (1111) & g^{13} &= (1101) & g^{14} &= (1001) & g^{15} &= (0001) \end{aligned}$$

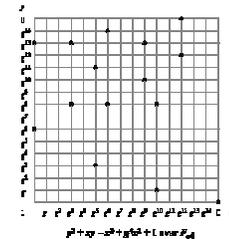
Is (g^5, g^3) a point on the curve?

$$(g^3)^2 + g^3g^3 = (g^3)^3 + g^4(g^3)^2 + 1$$

$$g^6 + g^6 = g^{15} + g^{14} + 1$$

$$(1100) + (0101) = (0001) + (1001) + (0001)$$

$$(1001) = (1001)$$



CNS Lecture 9 - 16

ECC challenge

- Certicom challenge over Z_p and/or over $GF(2^m)$
- | Challenge | End Date | Elliptic Curve | Iterations | Machine | Days |
|-----------|----------------|----------------------|------------|-------------------|------|
| ECC2-79 | Dec. 16, 1997 | 1.7×10^{12} | 170000 | | 116 |
| ECC2-89 | Feb. 9, 1998 | 1.8×10^{13} | 187000 | | 114 |
| ECC2-95 | May 21, 1998 | 2.2×10^{13} | 149000 | | 1709 |
| ECC2-109 | April 27, 2004 | 2600 computers | | 17 months | |
| ECCp-79 | Dec. 6, 1997 | 1.4×10^{12} | 314000 | | 52 |
| ECCp-89 | Jan. 12, 1998 | 2.4×10^{13} | 388000 | | 716 |
| ECCp-97 | Mar. 18, 1998 | 2.0×10^{14} | 361000 | | 6412 |
| ECCp-109 | Nov 6, 2002 | | | 29.7M (50K x 594) | |

- ECC2-97 sept 99, ECC 97 bit private key found, 16000 MIPS-yr (more than 512-bit RSA challenge), used 740 computers, 40 days

Key Size	MIPS-Years
150	3.8×10^{10}
205	7.1×10^{18}
234	1.6×10^{28}

Key Size	MIPS-Years
512	3×10^9
768	2×10^9
1024	3×10^{11}
1280	1×10^{14}
1536	3×10^{16}
2048	3×10^{20}

equivalent key sizes			
Symmetric	RSA	ECC	ECC
40	400		
56	512		
64	768		
80	1024	160	
90	2048	210	
128	3072	256	
256	15360	512	

(a) Elliptic Curve Logarithms using the Pollard rho Method

(b) Integer Factorization using the General Number Field Sieve

CNS Lecture 9 - 17

Using ECC

- Excellent for hardware implementations
- OpenSSL supports ECC in the API and at the command level
 - ECCDH and ECCDSA over either $GF(p)$ or $GF(2^m)$
 - Lots of different curves with different strengths (160 to 571 bits)
 - API includes routines for encoding/conversion and SSL/TLS support
 - Commands for keygen/encodings
 - ECC in X509 certs
- OpenSSL ECC performance in https
 - Also see openssl speed
- The test of time?

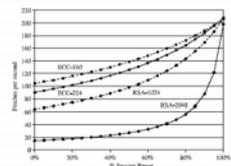


Figure 1: Throughput v/s session reuse plot.

CNS Lecture 9 - 18

ECC keys and OpenSSL

- Your ECC public/private key includes info describing the equation and coefficients $E_q(a,b)$ and base point G
- Your **private key** is a big random integer n (keep this secret)
- Your **public key** is the point on the curve nG (and equation info)
- The ECC standards (and OpenSSL) provide lots of "suitable" curves to choose from (see `openssl ecparam -list_curves`)
- To generate an ECC key pair

```
openssl ecparam -out ec_key.pem -name prime192v1 -genkey
```

and you can have a CA sign your public ECC key and create X509 cert

CNS Lecture 9 - 19



Your ECC keys

```
openssl ec -in ec_key.pem -noout -text
read EC key
Private-Key: (192 bit)
priv:
  56:7d:0a:64:7e:ed:44:b0:ea:2a:1a:90:3a:3c:d5:
  9e:47:1a:61:49:87:25:73:f8
pub:
  04:b0:d2:ca:ae:e9:d0:f8:f3:95:00:97:40:a3:d4:
  9b:89:2e:93:ab:bb:a2:49:75:ce:b2:22:a4:a6:be:
  9b:31:ae:10:f2:ce:a2:13:16:8d:61:c7:29:91:ab:
  27:56:10:50
ASN1 OID: prime192v1
```

Your pub key is actually a "point" (x,y), so there is some encoding
The OID tells the reader which equation used (p,a,b,G,n,h)

CNS Lecture 9 - 20



OpenSSL ECC API

- OpenSSL version 0.9.8 or later
- ECDH


```
EC_KEY *ecckey = EC_KEY_new_by_curve_name(nid);
const EC_GROUP *group;
group = EC_KEY_get0_group(ecckey);
EC_KEY_generate_key(ecckey); //pub key
EC_POINT_get_affine_coordinates_GFp(group,
EC_KEY_get0_public_key(ecckey), x, y, ctx)
ECDH_compute_key(...) // shared secret
```
- ECDSA


```
EC_KEY *key; ECDSA_SIG *signature;
EVP_DigestFinal(&md_ctx, digest, &dgst_len);
signature = ECDSA_do_sign(digest, 20, key);
if (ECDSA_do_verify(digest, 20, signature, key) != 1)
```

CNS Lecture 9 - 21



Public key crypto

- public key crypto meets our security requirements
 - privacy
 - integrity
 - authentication
 - non-repudiation
- choose from RSA, ElGamal, ECC or sign with DSA
- key agreement with D-H
- need random numbers, primes, generators, Big Integer software
- standards (IEEE P1363 and PKCS)
- symmetric-key crypto (DES, AES,...) still needed for speed
- Solves symmetric key distribution problem
 - but carrying your private key around is still a problem
- public key management (PKM) still unsolved ... (later)

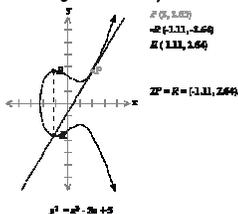
•Diffie-Hellman	Key agreement Discrete logs
•RSA	Sign/encrypt Factoring integers
•DSS	Sign Discrete logs
•ECC	Sign/encrypt/key agreement Elliptic curves

CNS Lecture 9 - 22



Number theory for crypto ✓

- Mod arithmetic, gcd, CRT (shift cipher, Hill, RSA, D-H, ECC)
- Polynomial arithmetic over $GF(2^n)$ (LFSR, ECC, AES, CRC)
- Primality tests, irreducible polynomials, generators
- Random number generation (keys, IV, blinding, k for DSS)
- BIG Integer** arithmetic
- Nonlinear Boolean functions (Bent)
- Factoring and discrete logs
- Elliptic curves
- Computational complexity



Security through mathematics

CNS Lecture 9 - 23



Crypto toolbox ✓

You have tools for building secure applications

- fast symmetric key encryption
- hash functions
- random numbers, prime testing
- public key crypto
- Big integer math libraries/methods
- algorithms for message authentication, key exchange, user authentication
- rules for encoding, padding, interoperability (more later)
- no standard API (more later)



next: applied crypto

CNS Lecture 9 - 24



Applied crypto – secure applications

security features ≠ secure features

Evaluation criteria

- privacy, integrity, availability
- encryption (symmetric and public key)
- message authentication (hashes)
- user authentication (mutual?)
- key size, distribution, re-new
- encoding/protocols
- random number generation
- prime generation
- API
- replay defense
- offline attacks
- Strong software engineering (secure design and coding)

CNS Lecture 9 - 25



SSH & PGP

ssh and pgp are sample applications that use public key crypto, hashing, symmetric key encryption, random numbers, and do their own public key management

- #### ssh
- crypto negotiation
 - session key establishment
 - authentication protocols
 - public and secret key
 - manual public key mgt.

- #### pgp
- message authentication/encryption
 - public and secret key
 - user-based key certification and mgt., key rings, trust
 - Message envelopes



CNS Lecture 9 - 26



ssh

Secure Shell

- public domain encrypted shell
- runs on most UNIX systems
- Windows client
- replaces rsh rlogin rcp ftp
- can tunnel other TCP services (X)
- developed in Finland, now OpenSSH
- uses RSA/DSS, DES/3DES/IDEA/RC4/Blowfish/TSS
- optional compression (gzip)
- v1 uses crc32 for MAC (encrypted)
- Newer versions based on OpenSSL lib (not SSL protocol)

components: sshd ssh scp ssh-keygen ssh-agent sftp

SSH features

- strong/mutual authentication (RSA)
- defeats IP impersonation and DNS hacks
- encryption defeats session hijacking, passwords in the clear, privacy violations
- uses encrypted tunnel for other services
- public key generation and session key generation require strong random (unpredictable) numbers

CNS Lecture 9 - 27



ssh support files



HOST /etc/

- sshd_config what's allowed
- ssh_host_key ssh_host_key.pub (ssh_host_dsa_key) – at install time
- ssh_random_seed
- ssh_known_hosts
- (server key -- regenerated each hour, not saved)

USER .ssh/

- identity.d u p q u = p⁻¹ mod q
- identity.pub (ascii) bits e n
id_rsa or id_dsa (plus .pub) for OpenSSH
- random_seed
- known_hosts
hostname/pub key
- authorized_keys
pubkey + label

CNS Lecture 9 - 28



ssh config files

sshd_config -- what sshd will allow

```
Port 22
HostKey /etc/ssh_host_key
RandomSeed /etc/ssh_random_seed
ServerKeyBits 768
LoginGraceTime 600
KeyRegenerationInterval 3600
PermitRootLogin no
X11Forwarding yes
SyslogFacility DAEMON
RhostsAuthentication no
RhostsRSAAuthentication yes
RSAAuthentication yes
PasswordAuthentication yes
PermitEmptyPasswords yes
```

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ssh protocol



- TCP port 22 (sshd)
- server sends version info
- client replies with version info
- server sends host and server pub keys, cookie, supported encryption and authentication
- client checks known_hosts
- client selects and sends encryption mode, cookie, and random session key encrypted with host AND server pub key
- server sends confirmation encrypted with session key
- server is authenticated
- host key added to your known_hosts on client, warns if no match
- Subsequent messages:
 - Encrypted
 - CRC used for integrity (v1)
 - all messages have some random padding

Next, user authentication begins (either UNIX password or user RSA key)

- new server keys each hour

CNS Lecture 9 - 30



ssh authentication



- **Installation generates host pub/priv key** `ssh-keygen`
- **RSA host authentication (mutual)**
 - use `.rhosts/.shosts` or `hosts.equiv`
 - Server or user's `known_hosts` must have client host's pub key
 - server sends random challenge (cookie) encrypted with client host's pub key
 - client responds with MD5 hash of challenge
- **user RSA authentication**
 - user generates pub/priv key `ssh-keygen`
 - stored in `.ssh/`
 - private key encrypted with IDEA/3DES using `passphrase`
 - authorized keys in your `ssh/` on server
 - server sends random challenge (cookie) encrypted with your pub key
 - client responds with MD5 hash of challenge
- **UNIX password (but session is already encrypted)**
- **Handy authentication agent (ssh-agent) - only type your passphrase once**
 - E.g. in login start your X server with `ssh-agent startx`
 - When you start login, from an xterm, `ssh-add` (asks for your passphrase)
 - All `ssh` commands using user-RSA key will be handled automatically

CNS Lecture 9 - 31



An ssh (v1) session

```
ssh -v
SSH Version 1.2.17 [i686-unknown-linux], protocol version 1.5.
Standard version. Does not use RSAREF.
Reading configuration data /etc/ssh_config
ssh connect: getuid 23673 geteuid 0 anon 0
Connecting to whisper [128.169.93.200] port 22.
Allocated local port 1022.
Connection established.
Remote protocol version 1.5, remote software version 1.2.26
Waiting for server public key.
Received server public key (768 bits) and host key (1024 bits).
Host 'whisper' is known and matches the host key.
Initializing random; seed file /home/thistle/dunigan/.ssh/random_seed
Encryption type: idea
Sent encrypted session key.
Received encrypted confirmation.
Trying rhosts or /etc/hosts.equiv with RSA host authentication.
Remote: Rhosts/hosts.equiv authentication refused: client user 'dunigan',
server user 'dunigan', client host 'thistle.epm.ornl.gov'.
Server refused our rhosts authentication or host key.
No agent.
Trying RSA authentication with key 'dunigan@icarus'
Received RSA challenge from server.
Enter passphrase for RSA key 'dunigan@icarus':
```

CNS Lecture 9 - 32



Random numbers in ssh

- Used for prime generation/testing, cookie, session key
- From `random.c`

```
random_get_noise_from_command(state, uid, "ps laxw 2>/dev/null");
if (time(NULL) - start_time < 30)
    random_get_noise_from_command(state, uid, "ps -al 2>/dev/null");
if (time(NULL) - start_time < 30)
    random_get_noise_from_command(state, uid, "ls -alni /tmp/. 2>/dev/null");
if (time(NULL) - start_time < 30)
    random_get_noise_from_command(state, uid, "w 2>/dev/null");
if (time(NULL) - start_time < 30)
    random_get_noise_from_command(state, uid, "netstat -s 2>/dev/null");
if (time(NULL) - start_time < 30)
    random_get_noise_from_command(state, uid, "netstat -an 2>/dev/null");
if (time(NULL) - start_time < 30)
    random_get_noise_from_command(state, uid, "netstat -in 2>/dev/null");
```
- then mixes using MD5, some randomness saved in file `random_seed`
- uses GNU's multiprecision library
- Openssh uses openssl lib's for random (based on `/dev/random`)

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Prime tests in ssh

Generating primes p and q for RSA (`rsa.c`)

- generate big-integer random number
- set 2 highest bits, low bit
- See if divisible by small primes (1050) (print . if passed test)
- fermat test for witness 2
 - not prime if $2^n \bmod n \neq 2$
 - if passed test, print +
- 20 Miller-Rabin tests (GMP)
 - print + (distance is number of tries x 2)
- confirm $p \neq q$ and not too close and are relatively prime
- confirm RSA encrypt/decrypt works
- If any of the tests fail, generate a new random number (+2) and start over ...

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Key generation

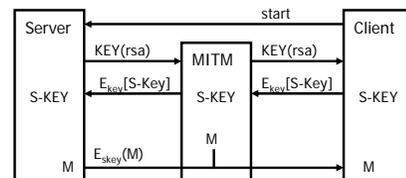
```
cetus3a% ssh-keygen -b 1024 -f test -N ''
Initializing random number generator...
Generating p: .....
.....+ (distance 1046)
Generating q: .....+ (distance 114)
Computing the keys...
Key generation complete.
Your identification has been saved in test.
Your public key is:
1024 33 14393845200713617792488580070948770049655935640447464542973550523411925
988626432231834904178177361003974229009395891439634525760727235660285
82461520936180182589295082705770544338981030800374712927386236806723033247571
5862471519863545171529247567102098771947439443619083792269274291408340652383
dunigan@cetus3a
Your public key has been saved in test.pub
```

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SSH v1 vulnerabilities

- Cipher text exposes size of username and password
- Vulnerable to man-in-the-middle attack
 - Assumes client doesn't have server's key already
- Use v2



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ssh updates



- `ssh v2` (OpenSSH)
- SecurID, s/key, and Kerberos support
- blowfish, AES, RC4
- SHA1
- D-H, DSA
- use `/dev/random` and OpenSSL's libssl
- new protocols, `sftp`
- uses hash (hmac-md5 or hmac-sha) instead of CRC
- `speedups`
- IETF's secure shell (`ssch`)
- Also versions that will use public key/`ssh` or one-time passwords (`fob`)
- **Use `ssh` and get latest version (there are/have been bugs/holes)**

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PGP implementation



- key generation
- files and key representation (`pgformat.doc`)
- signatures
- encryption
- encoding (radix-64 ASCII)
- trust model
- uses RSA, IDEA, MD5, ZIP (DSA, 3DES with GnuPG)
- big number lib (`mpilib.c`)
- multi OS, multi architecture
- RFC 3156

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PGP services

- Tool for encrypting/signing files
- Used with email
- Based on public keys and a web of trust

Function	Algorithms Used	Description
Digital signature	DSS/SHA or RSA/SHA	A hash code of a message is created using SHA-1. This message digest is encrypted using DSS or RSA with the sender's private key and included with the message.
Message encryption	CAST or IDEA or Three-key Triple DES with Diffie-Hellman or RSA	A message is encrypted using CAST-128 or IDEA or 3DES with a one-time session key generated by the sender. The session key is encrypted using Diffie-Hellman or RSA with the recipient's public key and included with the message.
Compression	ZIP	A message may be compressed, for storage or transmission, using ZIP.
Email compatibility	Radix 64 conversion	To provide transparency for email applications, an encrypted message may be converted to an ASCII string using radix 64 conversion.
Segmentation	-	To accommodate maximum message size limitations, PGP performs segmentation and reassembly.

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PGP keys

- select a distinguished name (user id)
- initially generate RSA public/private key pair
 - key strokes for random source (original PGP)
 - find RSA primes and exponents
 - large integers (1024 bit)
- private key encrypted with IDEA/AES using passphrase in `.pgp/secring.pgp` (`gnupg/` for GnuPG)
- public key and other's public keys on your public key ring `.pgp/pubring.pgp`
- keyid is last 64 bits of RSA modulus n
- key fingerprint is MD5 hash of public key (verifier)

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PGP keys

public key

- creation timestamp
- validity period
- algorithm (RSA)
- modulus n
- exponent e

user id

- length of userid string
- ASCII userid (e.g. email address)

Can have multiple userids associated with a public key

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private key

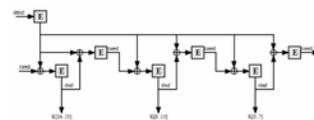
- creation timestamp
- validity period
- algorithm (RSA)
- modulus n
- exponent e
- secret exponent d
- factor p
- factor q
- $u = p^{-1} \text{ mod } q$

Multiprecision integers: number of bits (16-bit number), bytes (MSB first)



Random numbers in PGP

- Used for key generation, session keys, IV
- `noise.c` `random.c` `randpool.c` (v 2.6.2)
 - key strokes, high res time (`dtbuf`)
 - randomness retained in `randseed.bin` (`reseed`)
 - data from file pre/post washed with CFB
 - updated any time user does keyboard input
 - updated with MD5 of file being encrypted
 - data stirred with MD5
 - uses X9.17 but with CAST-128
 - `randseed.bin` updated



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gpg randomness

- Random numbers for public key generation and message keys
- `cipher/random.c` based on Gutman's paper
- Uses `/dev/urandom`, seed file + pid, time, and clock
- Mixes pool with RIPEMD-160
- Wipes stack and prefers "secure memory" (no swap)
- Pool updated whenever key requested for encryption or secure hash (DSS k)
- Stats track current entropy of pool
- Application can request strong entropy (slower)
- Saves pool to file `~/.gnupg/random_seed`

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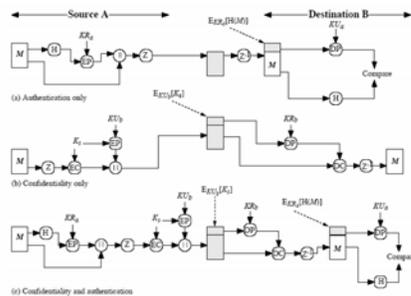
PGP primes

- `genprime.c`
- generate random n-bit number p
- set two hi-bits to 1, use 3 mod 4 numbers (Blum)
- verify p is not divisible by all primes less than 2000
- perform four Fermat tests, for any random x
 - if $x^{p-1} \bmod p \neq 1$ then p is not prime
 - if fails, add 4 and try again
- find prime q that is not too close to p
- verify RSA encrypt/decrypt works!
- this is what takes time when you first generate your PGP keys

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PGP crypto



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PGP signatures

- Signing a message (-sat)
 - hash (MD5) message, sig type, and time
 - encrypt hash plus some padding with your private key (PKCS 1)
 - encode in radix-64 ASCII for email transport (canonical)
 - includes 24-bit CRC with pad (version 1)
 - receiver can verify by re-computing hash, decrypting signature with your public key and comparing hash values
- -sa uses ASCII encoding (NOT encryption), need PGP to decode
- -sat leaves in clear text, don't need PGP to read,

To make a detached signature file (e.g., for authentication of a tar file)

```
gpg -sb mystuff.tar
```

Creates mystuff.tar.sig



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PGP signature

signature type
timestamp
key id of signer (64 bits)
algorithm (RSA, MD5)
verifier (first 2 bytes of hash)
encrypted hash

Encrypted hash is RSA-encrypted multiprecision integer

Signing a key (-ks)

says you believe this public key is associated with this user id

- hash (MD5) of public key pkt and user id pkt, sig type, and time
- encrypt hash plus some random padding with your private key (ref PKCS 1)

signed key is a "certificate"

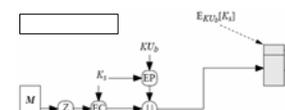
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PGP encryption

Encrypting a message (-ea)

- generate a message key (random)
- compress (ZIP) message
- encrypt message with message key
 - IDEA, 64-bit CFB (faster than RSA)
 - IV of 0
 - 8 random bytes, verifier (2B), message
- encrypt (RSA) message key with recipient's public key (one per recipient)
 - keyid (64 bits)
 - encrypted IDEA key (PKCS 1)
- encode in radix-64 ASCII (-a)



Encrypting a file (-c)

```
IDEA/3DES/AES
```

MD5 hashed passphrase as key

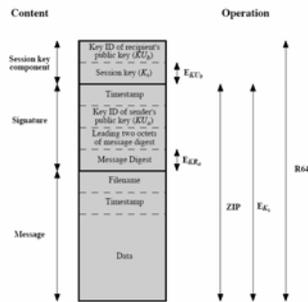
options for over-writing plaintext file

PGP is also careful about zeroing out secrets in memory.

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PGP message format



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PGP compression

- **Why compress?**
 - Hide plain text
 - Reduce message size
 - Faster encryption/decryption
 - Less storage space
 - Faster transmission
- **PGP compresses with ZIP**
 - Replaces repeated substrings with a short "code word"
 - Compressed data includes the code mappings and the compressed data

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PGP encoding – radix-64

- Encoding binary data as ASCII (*pgp, s/mime*) – keep mail programs happy
 - uuencode
 - radix-64
- radix-64 encodes 6-bits at a time (6 bits to 8-bit character)

6-bit value	character encoding						
0	A	16	Q	32	g	48	w
1	B	17	R	33	h	49	x
2	C	18	S	34	i	50	y
3	D	19	T	35	j	51	z
4	E	20	U	36	k	52	0
5	F	21	V	37	l	53	1
6	G	22	W	38	m	54	2
7	H	23	X	39	n	55	3
8	I	24	Y	40	o	56	4
9	J	25	Z	41	p	57	5
10	K	26	a	42	q	58	6
11	L	27	b	43	r	59	7
12	M	28	c	44	s	60	8
13	N	29	d	45	t	61	9
14	O	30	e	46	u	62	-
15	P	31	f	47	v	63	/
						(pad)	=

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Attacking PGP

- **Decrypting a message**
 - attack 3DES/IDEA/blowfish
- **Recover the message key encrypted with the receiver's pub key**
 - attack RSA
 - attack random number generator/protocol
- **Forge a message**
 - attack RSA
 - find collision on MD5/SHA
- **Steal your private-key file**
 - Attack symmetric key encryptor (3DES etc.)
 - Dictionary attack on your passphrase
- **Keyboard sniffer to get your passphrase**
- **Trojan horse to get your passphrase**



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PGP trust

How do you know it's Tom's key?

- verify key (voice, fingerprint)
- or someone you "trust" has signed it (a "certificate")
- PGP asks you (or *gpg --edit-key*)
 - Do you want to certify any of these keys yourself (y/N)?
 - Are you sure key belongs to xxxx?
 - Would you trust xxxx as an introducer (1-4)?

• two trusted objects

- certainty of key (KEYLEGIT). It is Bob's key
- trust in user as an introducer (OWNERTRUST)

Trust levels
1. I don't know
2. I do NOT trust
3. I trust marginally
4. I trust fully

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PGP web of trust

- key is trusted if signed by people/keys you trust
- PGP will recalculate trust periodically
- key may become trusted if "enough" good certificates
- extracted key includes certificates (key envy) (no trust info)
- key signing parties
- what if no trust?
- compromised keys (sig type)
- scalable?
- web/mail key servers (Bill Clinton)
 - Lots of signatures saying it's legit (JoeTheHacker, BobTheHacker ...)
- When you sign Bob's key, you're saying you trust that this key belongs to Bob.
- Will contrast with certificates signed by a Certificate Authority (CA) and a formal Public Key Infrastructure (PKI)

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ASN.1/DER encoding used for X509 certs

- ASN.1 – notation for describing data structures (C-like)
- Distinguished Encoding Rules (DER) subset of Basic Encoding Rules (BER)
Tag, length, value encoding for strings, big integers, date, time, etc.
platform-independent data representation

```
0x01 -- [0000 0001], [BOOLEAN] GetRequest.lock
0x01 -- [0000 0001], length 1
0x00 -- [0000 0000] value FALSE

0x04 -- [0000 0100], [OCTET STRING] GetRequest.url
0x16 -- [0001 0110], length 22
[/ses/magic/moxen.html] - value
```

Slow/ugly in software (libraries provided in OpenSSL)

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X509v3 ASN.1 cert

```
Certificate ::= SEQUENCE {
    tbsCertificate TBSCertificate,
    signatureAlgorithm AlgorithmIdentifier,
    signatureValue BIT STRING
}
```

```
TBSCertificate ::= SEQUENCE {
    version [0] EXPLICIT Version DEFAULT v1,
    serialNumber CertificateSerialNumber,
    signatureAlgorithmIdentifier,
    issuerName,
    validity Validity,
    subject Name,
    subjectPublicKeyInfo SubjectPublicKeyInfo,
    issuerUniqueId [1] IMPLICIT UniquelyIdentifier OPTIONAL,
    -- If present, version shall be v2 or v3
    subjectUniqueId [2] IMPLICIT UniquelyIdentifier OPTIONAL,
    -- If present, version shall be v2 or v3
    extensions [3] EXPLICIT Extensions OPTIONAL,
    -- If present, version shall be v3
}
```

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X509 in OpenSSL

- Create RSA pub/private key (no protection on private key)
- Saved in PEM format file (later)
- You can also pre-specify info in a config file for openssl

```
openssl req -new -x509 -days 3650 -nodes -out mycert.pem -keyout mykey.pem
Generating a 1024 bit RSA private key
.....+++++
writing new private key to 'mykey.pem'
-----
You are about to be asked to enter information that will be incorporated
into your certificate request.
What you are about to enter is what is called a Distinguished Name or a DN.
There are quite a few fields but you can leave some blank
For some fields there will be a default value,
If you enter '.', the field will be left blank.
-----
Country Name (2 letter code) [GB]:US
State or Province Name (full name) [Berkshire]:TN
Locality Name (eg, city) [Newbury]:Knoxville
Organization Name (eg, company) [My Company Ltd]:UT
Organizational Unit Name (eg, section) []:CS
Common Name (eg, your name or your server's hostname) []:Bubba
Email Address []:bubba@utk.edu
```

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X509 in OpenSSL (examining a certificate)

```
openssl x509 -in mycert.pem -text -noout
Certificate:
    Data:
        Version: 3 (0x2)
        Serial Number: 0 (0x0)
        Signature Algorithm: md5WithRSAEncryption
        Issuer: C=US, ST=TN, L=Knoxville, O=UT, OU=CS, CN=Bubba/emailAddress=bubba@utk.edu
        Validity
            Not Before: Apr 21 21:55:08 2006 GMT
            Not After : Apr 18 21:55:08 2016 GMT
        Subject: C=US, ST=TN, L=Knoxville, O=UT, OU=CS,
        CN=Bubba/emailAddress=bubba@utk.edu
        Subject Public Key Info:
            Public Key Algorithm: rsaEncryption
            RSA Public Key: (1024 bit)
            Modulus (1024 bit):
                00:e5:a1:29:2f:89:7c:08:24:2e:22:55:1c:04:01:
                f4:68:52:f7:94:59:3b:c4:d8:82:01:65:c9:db:88:
                ..
                cc:51:8c:32:98:5c:a9:b7:2f
            Exponent: 65537 (0x10001)
        X509v3 extensions:
            X509v3 Subject Key Identifier:
                A7:A1:3F:1D:47:BC:C9:01:CL:78:AD:D1:5C:72:86:C3:81:5A:21:44
            X509v3 Authority Key Identifier:
                keyId:A7:A1:3F:1D:47:BC:C9:01:CL:78:AD:D1:5C:72:86:C3:81:5A:21:44
                DirName:/C=US/ST=TN/L=Knoxville/O=UT/OU=CS/CN=Bubba/emailAddress=bubba@utk.edu
                serial:00
            X509v3 Basic Constraints:
                CA:TRUE
        Signature Algorithm: md5WithRSAEncryption
            9e:f1:29:9a:17:0f:d5:90:2a:e2:04:8c:1a:7d:42:9e:72:20: ...
```

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ECC in X509 cert

```
Certificate:
    Data: Version: 1 (0x0) Serial Number: ed:f9:85:3f:69:9e:ac:e1
    Signature Algorithm: ecdsa-with-SHA1
    Issuer: C=US, ST=CA, L=Mountain View, O=Sun Microsystems
    Validity Not Before: Dec 6 21:30:14 2005 GMT
    Not After : Jan 14 21:30:14 2010 GMT
    Subject: C=US, ST=CA, L=Mountain View, O=Sun Microsystems
    Subject Public Key Info:
    Public Key Algorithm: id-ecPublicKey Public-Key: (161 bit)
    pub:
    04:eb:e0:7c:77:eb:bf:f7:95:d0:41:89:35:7f:e9:
    67:d5:b9:a4:63:55:85:2b:16:d7:17:2e:ab:05:d3:
    8c:f7:c8:bd:dd:c3:84:dc:cl:29:d0
    ASN1 OID: secP160r1
    Signature Algorithm: ecdsa-with-SHA1
    30:2d:02:15:00:80:81:d1:c8:84:88:18:ee:76:44:b9:33:e4:
    e0:0d:1a:30:4b:dc:2a:02:14:31:76:dd:e9:26:83:4c:72:1d:
    2c:04:6b:f2:66:fa:4f:12:a5:b8:94
    -----BEGIN CERTIFICATE-----
    MIICBCCMIIODQD+YU/a664fA/BgqhkhjOPQRMIGrMQewCQYDUVQQBwJVUsEL
    MAKGAUUECAwQCEXfjAUBgNVAwMDU1vM50YUW1UfzPzCcxJjAkBgNVBAoMHRVNL
    ....
    SM49BAEDMAAwLQ1VAICB0ciEiBjjudkS5M+TgDRowS9wqAhQxdt3pJnMch0sBGvy
    ZvpPEqW41a==
    -----END CERTIFICATE-----
```

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PKCS

Public-Key Cryptography Standard

- encoding standard (not really, owned/motivated by RSA)
- How to encode public keys (big integers), signatures, algorithms
 - Rules for padding
- uses ASN.1
- (1) RSA encodings
 - (3) Diffie-Hellman
 - (5) secret key encryption
 - (6) key certificate syntax (deprecated by X.509v3)
 - (7) digital envelopes (see also IETF PKIX CMS)
 - (8) private key syntax
 - (9) attributes for C, T, E, IO
 - (10) certification request format
 - (11) crypto token API (competitor: Microsoft CSP)
 - (12) key file format
 - (13) ECC (signature, key agreement, encryption, encoding, algorithms)
 - (14) Pseudo random number generation
 - (15) Crypto tokens

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PKCS 1 RSA

How to use RSA (RFC 2437) encodings for

- public key/private key
- signature
- short encrypted message (key)
- short signed message (MAC)

Format of message to be encrypted (bytes)

```
0 1 2 3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9
-----
|0|2|8-random bytes |0| data (e.g., session key)
-----
```

Format of message to be signed

```
0 1 2 3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9
-----
|0|1|8 bytes of FF |0| ASN.1 digest type and digest
-----
```

deals with several threats

- random padding defeats guessable messages
- diff. padding for each recipient defeats multiple copies when $e=3$
- numbers not smooth (small primes)
- interoperable encodings

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PKCS 5 – secret key

Password-Based Cryptography Standard

- Version 1.5, 1993, Version 2.0, 1999
- Oriented towards protection of private keys
- Does not specify a standard for password format
- Protocols for salt, hash, padding
- Encryption schemes
 - PBES1 with DES or RC2 in CBC plus padding
 - PBES2 with arbitrary encryption scheme
- MAC scheme

Pad with 1 to blocksize bytes
Pad value is number of pad bytes
x x x x x 3 3 3
If plaintext multiple of blocksize,
then an extra block is added.
Example, OpenSSL EVP

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PKCS 7 – crypto message syntax

- Compatible with PEM, uses ASN.1 and BER (tag,length,value)
- Syntax for digital signatures and envelopes (recursive)
- 6 content types
data, signed data, enveloped data, signed-enveloped data, digested data, encrypted data

```
EnvelopedData ::= SEQUENCE {
    version Version,
    recipientInfos RecipientInfos,
    encryptedContentInfo EncryptedContentInfo }
RecipientInfos ::= SET OF RecipientInfo
EncryptedContentInfo ::= SEQUENCE {
    contentType ContentType,
    contentEncryptionAlgorithm ContentEncryptionAlgorithmIdentifier,
    encryptedContent [0] IMPLICIT EncryptedContent OPTIONAL }
```

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PKCS 8 – private key syntax

PrivateKeyInfo

- version
- privateKeyAlgorithm
- privateKey
- Attributes
- encryptedPrivateKeyInfo
 - encryptionAlgorithm
 - encryptedData
- privateKeyInfo BER-encoded and encrypted
- Usually encrypted using PKCS 5

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PKCS 10 – certification request

- Certification Request
 - certificationRequestInfo
 - Version, subjectName, subjectPublicKeyInfo, attributes
 - signatureAlgorithm
 - signature
- Signed with private key corresponding to public key in request
- very RSA specific
- RFC 2511 defines a different format:
certificate request message format

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PKCS 12 – personal info exchange format

Example: IE/netscape personal key export

types of information

- PKCS 8 shrouded key
- Private key
- Certificates
 - X.509v3
 - SDSI
- CRLs
 - X.509
- Secret
 - Whatever

Each of these can be

- Plaintext
- Enveloped
 - encrypted using a secret key which is encrypted using a public key
- Encrypted
 - secret key encrypted
 - usually password derived
 - use PKCS 5 and a password formatting standard which is part of PKCS 12

recursive composition of these

The entire stuff is then either

- Signed and accompanied with signing certificate
- MACed
 - PKCS 5 based and accompanied with salt and iteration count

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